Lifetime Income Inequality: quantile treatment effect of retirement on the distribution of lifetime income.

Małgorzata Karolina Kozłowska

University of Warsaw

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Life cycle, social security and inequality

- Human Capital Earnings Function (HCEF)
 - Fanning out of earnings profiles across education groups as the cohort ages.
- Permanent Income Hypothesis (PIH)
 - Within cohort inequality evolves over life-cycle, reaching the highest levels in the old age.
 - Disparities in earnings between groups with different schooling levels grow in retirement age.
 - Reducing the share of income that is transferred through Social Security Systems increases life cycle inequality.
- Social Welfare Theory (SW)
 - By Pigou-Dalton Principal of Transfers any (mean-preserving) progressive transfer decreases inequality.

Research questions

- What is the impact of staying longer in labor force on distribution of lifetime income ?
- What is the impact of postponing retirement age on lifetime income inequality ?

Survey of Health Aging and Retirement

- Multidisciplinary cross-country longitudinal survey that collects micro data on individuals aged 50+.
- The data used in this study consists of two regular panel waves followed by the life history questionnaire of which the data were collected accordingly in 2004-2005, 2006-2007 and 2008-2009.
- This study covers 10 European countries: Austria, Germany, Sweden, The Netherlands, Spain, Italy, France, Denmark, Switzerland, Belgium.
- The sample is constrained to males who at the moment of the interview are retired.

Lifetime income

Measure of lifetime income

$$Y_i = \sum_{j=1}^{R_i} \omega_j W_{ij} + \sum_{R_i+1}^{110} s_{j+1} \omega_j P_{ij}$$

where:

 Y_i - total lifetime income

 W_{ij} - lifetime earnings from work at age j

 P_{ij} - lifetime retirement pension at age j

R_i - retirement age

 s_{j+1} - probability of surviving to age j+1, predicted based on Lee-Carter model

 ω_i - discount rate (2% to age 50)

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Deriving lifetime earnings from SHARE

Earnings model:

$$\ln w_{it} = \alpha_0 + \rho S_i + \beta_1 E_{it} + \beta_2 E_{it}^2 + \beta_3 E_{it}^3 + \beta_4 E_{it}^4 + \varepsilon_{it}$$

where:

- In wit log of earnings
- S_i years of schooling
- Eit number of years of experience

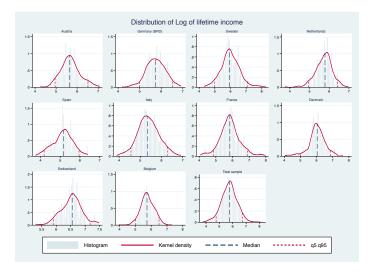
Prediction equation:

$$\widehat{\ln w_{it+1}} = \ln w_{it} + b_1(E_{it+1} - E_{it}) + b_2(E_{it+1}^2 - E_{it}^2) + b_3(E_{it+1}^3 - E_{it}^3) + b_4(E_{it+1}^4 - E_{it}^4)$$

Retransformation of predictions of earnings in logarithm to predictions in levels:

$$Q^{(p)}(y|x) = exp\{Q^{(p)}[log(y)|x]\}$$

Kernel density estimates

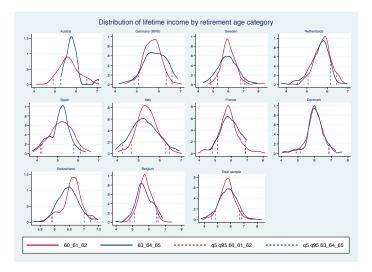


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Kernel density estimates by retirement age



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Model specification

Specification of the model in a cross-country setting:

$$Y_i = \alpha_0 + \alpha_1 R_i + \beta^\top X + \varepsilon_i$$
$$Q_\tau(Y_i) = \alpha_{0\tau} + \alpha_{1\tau} R_i + \beta_\tau^\top X$$

where:

 Y_i - personal lifetime income

 R_i - binary indicator taking value 1 if an individual retired exactly at age 63 or later, and 0 if an individual retired by age 62

X - set of country and cohort dummies.

Estimation and identification

- Issues : Endogenity
- Identification: Quantile Instrumental Variables techniques
 - Abadie, Angrist & Imbens (2002)
 - Chernozukov & Hansen (2005)
- Instruments: legislated early and normal retirement ages differenced with age:

$$\begin{cases} \mathsf{Z=1}, & \text{if } \mathsf{A}_i - \textit{leg}_{\textit{ER}} \geq 3 \\ \mathsf{Z=0}, & \text{if } \mathsf{A}_i - \textit{leg}_{\textit{ER}} < 3 \end{cases}$$

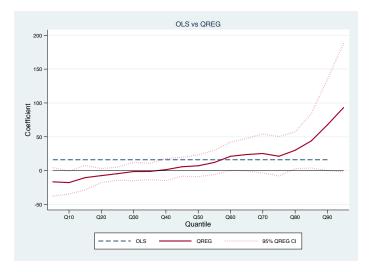
where:

 A_i is the actual age of an individual in the year of the interview,

 leg_{ER} is the earliest legal retirement age that an individual is eligible for.

Image: Image:

Ordinary Least Squares Estimates vs. Ordinary Quantile Regression



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Results

Quantile Regression vs. Quantile Treatment Effect (AAI)



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Results

Quantile Treatment Effect by the two estimators QTE-AAI and QIV-ChH



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Conclusions

- Clearly heterogenous, redistributive effect of postponing retirement to later ages across the quantiles of lifetime income in the overall sample.
- Extending working lives spreads out inequality in lifetime resources.
- The vast majority of people gain from working longer!